

CO₂/H₂O/痕量生态系统交换方程:
Yang et al 方程的推导解析及其应用讨论





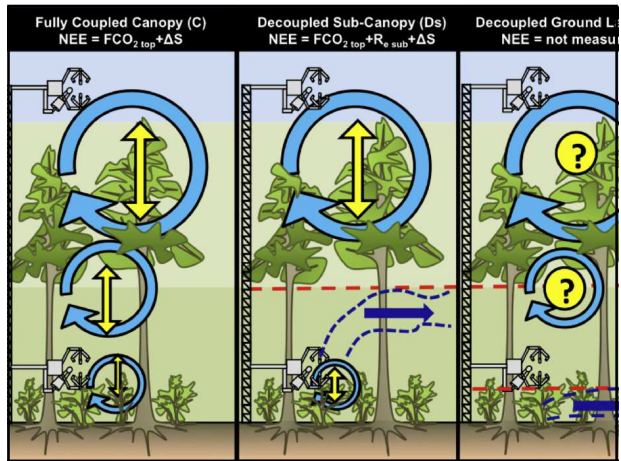
周新华¹ 王兴昌²
¹ Campbell Scientific, US; ² 东北林业大学
 第14次 ChinaFLUX 通量理论与技术培训
 2019年8月6日

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水汽滞留时间不确定，也可经平流远途运输后进入大气

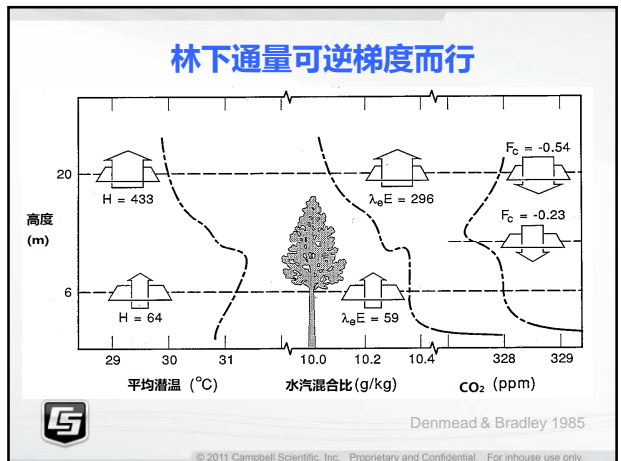
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林内的源和汇使林内通量复杂化

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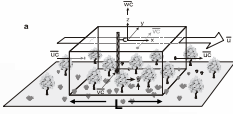


NEE: Net Ecosystem Exchange (净生态系统交换)
 生态系统中动植物包括土壤及微生物与其环境之间的单位面积CO₂平衡量 (生态系统吸收为负值, 排出为正值)。




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Full mass balance on a control volume



$$\begin{aligned} \bar{F}_c = \bar{F}_0 + \int_0^h \bar{S}_c dz &= \frac{1}{L^2} \int_0^L \int_0^L \int_0^h \bar{c}_d \frac{\partial \bar{\chi}_c}{\partial t} dx dy dz \\ &+ \frac{1}{L^2} \int_0^L \int_0^L \int_0^h \left[\bar{u} c_d \frac{\partial \bar{\chi}_c}{\partial x} + \bar{v} c_d \frac{\partial \bar{\chi}_c}{\partial y} + \bar{w} c_d \frac{\partial \bar{\chi}_c}{\partial z} \right] dx dy dz \\ &+ \frac{1}{L^2} \int_0^L \int_0^L \int_0^h \left[\frac{\partial c_d \bar{u}' \bar{\chi}_c'}{\partial x} + \frac{\partial c_d \bar{v}' \bar{\chi}_c'}{\partial y} + \frac{\partial c_d \bar{w}' \bar{\chi}_c'}{\partial z} \right] dx dy dz \end{aligned}$$

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$$S(t, x, y, z) = \frac{d\rho(t, x, y, z)}{dt}$$

$$d\rho = \frac{\partial \rho}{\partial t} dt + \frac{\partial \rho}{\partial x} dx + \frac{\partial \rho}{\partial y} dy + \frac{\partial \rho}{\partial z} dz$$

$$\frac{d\rho}{dt} = \frac{\partial \rho}{\partial t} + \frac{\partial \rho}{\partial x} \frac{dx}{dt} + \frac{\partial \rho}{\partial y} \frac{dy}{dt} + \frac{\partial \rho}{\partial z} \frac{dz}{dt}$$

$$S = \frac{\partial \rho}{\partial t} + u \frac{\partial \rho}{\partial x} + v \frac{\partial \rho}{\partial y} + w \frac{\partial \rho}{\partial z}$$

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Reynolds 平均与分解 (感谢杨柏)

$$S = \frac{\partial \rho}{\partial t} + u \frac{\partial \rho}{\partial x} + v \frac{\partial \rho}{\partial y} + w \frac{\partial \rho}{\partial z}$$

$$\begin{aligned} \rho &= \bar{\rho} + \rho' \\ S &= \bar{S} + S' \\ u &= \bar{u} + u' \\ v &= \bar{v} + v' \\ w &= \bar{w} + w' \end{aligned}$$

$$\bar{S} + S' = \frac{\partial(\bar{\rho} + \rho')}{\partial t} + (\bar{u} + u') \frac{\partial(\bar{\rho} + \rho')}{\partial x} + (\bar{v} + v') \frac{\partial(\bar{\rho} + \rho')}{\partial y} + (\bar{w} + w') \frac{\partial(\bar{\rho} + \rho')}{\partial z}$$

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$$\bar{S} + S' = \frac{\partial(\bar{\rho} + \rho')}{\partial t} + (\bar{u} + u') \frac{\partial(\bar{\rho} + \rho')}{\partial x} + (\bar{v} + v') \frac{\partial(\bar{\rho} + \rho')}{\partial y} + (\bar{w} + w') \frac{\partial(\bar{\rho} + \rho')}{\partial z}$$

平均后再用Tensor notation:

$$\bar{S} = \frac{\partial \bar{\rho}}{\partial t} + (\bar{u}_j + u'_j) \frac{\partial(\bar{\rho} + \rho')}{\partial x_j}$$

展开后

$$\bar{S} = \frac{\partial \bar{\rho}}{\partial t} + \bar{u}_j \frac{\partial \bar{\rho}}{\partial x_j} + \bar{u}'_j \frac{\partial \bar{\rho}}{\partial x_j} + \bar{u}_j \frac{\partial \rho'}{\partial x_j} + \bar{u}'_j \frac{\partial \rho'}{\partial x_j}$$

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$$\bar{S} = \frac{\partial \bar{\rho}}{\partial t} + \bar{u}_j \frac{\partial \bar{\rho}}{\partial x_j} + \overline{u'_j \frac{\partial \rho'}{\partial x_j}}$$

对两个变量乘积求导

$$\overline{\frac{\partial u'_j \rho'}{\partial x_j}} = \bar{u}'_j \frac{\partial \bar{\rho}}{\partial x_j} + \rho' \frac{\partial \bar{u}'_j}{\partial x_j}$$

$$\bar{S} = \frac{\partial \bar{\rho}}{\partial t} + \bar{u}_j \frac{\partial \bar{\rho}}{\partial x_j} + \frac{\partial \bar{\rho} u'_j}{\partial x_j} - \rho' \left(\frac{\partial u'_j}{\partial x_j} \right)$$

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$$\bar{s} = \frac{\partial \bar{p}}{\partial t} + \bar{u}_j \frac{\partial \bar{p}}{\partial x_j} + \frac{\partial \bar{\rho} \bar{u}_j}{\partial x_j} - \bar{\rho} \left(\frac{\partial u_j}{\partial x_j} \right)$$

不可压气体

$$\frac{\partial u_j}{\partial x_j} = 0 \quad \frac{\partial \bar{u}_j}{\partial x_j} = 0 \quad \frac{\partial u_j}{\partial x_j} = \frac{\partial (\bar{u}_j + u'_j)}{\partial x_j} = \frac{\partial \bar{u}_j}{\partial x_j} + \frac{\partial u'_j}{\partial x_j} = 0$$

$$\frac{\partial u'_j}{\partial x_j} = 0$$

$$\bar{s} = \frac{\partial \bar{p}}{\partial t} + \bar{u}_j \frac{\partial \bar{p}}{\partial x_j} + \frac{\partial \bar{\rho} \bar{u}_j}{\partial x_j}$$



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$$\bar{s} = \frac{\partial \bar{p}}{\partial t} + \bar{u}_j \frac{\partial \bar{p}}{\partial x_j} + \frac{\partial \bar{\rho} \bar{u}_j}{\partial x_j}$$

$$\left| \frac{\partial \bar{\rho} \bar{u}_1}{\partial x_1} + \frac{\partial \bar{\rho} \bar{u}_2}{\partial x_2} \right| \ll \left| \frac{\partial \bar{\rho} \bar{u}_3}{\partial x_3} \right|$$

$$\bar{s} = \frac{\partial \bar{p}}{\partial t} + \bar{u}_j \frac{\partial \bar{p}}{\partial x_j} + \frac{\partial \bar{\rho} \bar{u}_3}{\partial x_3}$$



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$$\bar{s} = \frac{\partial \bar{p}}{\partial t} + \bar{u}_j \frac{\partial \bar{p}}{\partial x_j} + \frac{\partial \bar{\rho} \bar{u}_3}{\partial x_3}$$

在单位面积上垂直积分至观测高度

$$\int_0^{h_m} \bar{s} dx_3 = \int_0^{h_m} \frac{\partial \bar{p}}{\partial t} dx_3 + \int_0^{h_m} \bar{u}_j \frac{\partial \bar{p}}{\partial x_j} dx_3 + \int_0^{h_m} \frac{\partial \bar{\rho} \bar{u}_3}{\partial x_3} dx_3$$

$$NEE = \int_0^{h_m} \frac{\partial \bar{p}}{\partial t} dx_3 + \int_0^{h_m} \bar{u}_j \frac{\partial \bar{p}}{\partial x_j} dx_3 + \left. \bar{\rho} \bar{u}_3 \right|_{x_3=h_m}$$

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$$NEE = \int_0^{h_m} \frac{\partial \bar{p}}{\partial t} dx_3 + \int_0^{h_m} \bar{u}_j \frac{\partial \bar{p}}{\partial x_j} dx_3 + \left. \bar{\rho} \bar{u}_3 \right|_{x_3=h_m}$$

再写为传统表达方式

$$NEE = \int_0^{h_m} \frac{\partial \bar{p}}{\partial t} dz + \int_0^{h_m} \left(\bar{u} \frac{\partial \bar{p}}{\partial x} + \bar{v} \frac{\partial \bar{p}}{\partial y} + \bar{w} \frac{\partial \bar{p}}{\partial z} \right) dz + \left. \bar{\rho} \bar{w} \right|_{z=h_m}$$



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IRGASON AP200

$$NEE = \int_0^{h_m} \frac{\partial \bar{p}}{\partial t} dz + \int_0^{h_m} \left(\bar{u} \frac{\partial \bar{p}}{\partial x} + \bar{v} \frac{\partial \bar{p}}{\partial y} + \bar{w} \frac{\partial \bar{p}}{\partial z} \right) dz + \left. \bar{\rho} \bar{w} \right|_{z=h_m}$$

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AP200 Profile System – Hawaii, USA


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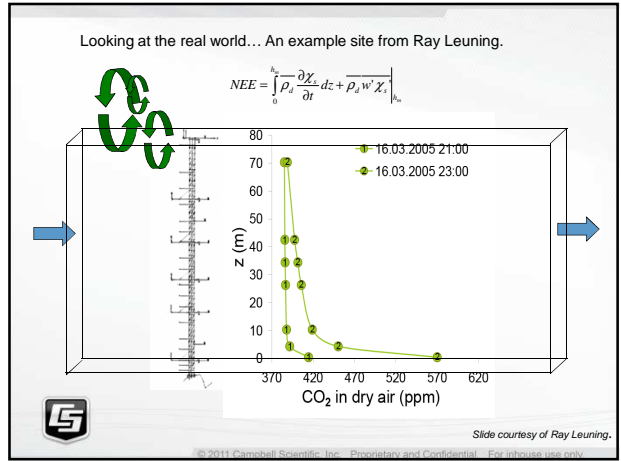
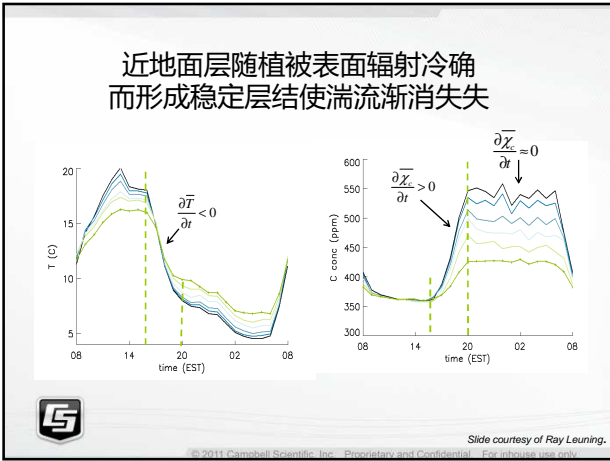


$$NEE = \int_0^{h_m} \frac{\partial \bar{p}}{\partial t} dz + \int_0^{h_m} \left(\bar{u} \frac{\partial \bar{p}}{\partial x} + \bar{v} \frac{\partial \bar{p}}{\partial y} + \bar{w} \frac{\partial \bar{p}}{\partial z} \right) dz + \overline{\rho w} \Big|_{z=h_m}$$

观察值计算模型

$$NEE = \sum_i \frac{\bar{\rho}_i(t_i) - \bar{\rho}_i(t_0)}{t_i - t_0} \frac{\Delta h_i}{h_m} + \sum_i \left(\bar{u}_i \frac{\bar{\rho}_i(t_i, x_i) - \bar{\rho}_i(t_0, x_0)}{x_i - x_0} + \bar{v}_i \frac{\bar{\rho}_i(t_i, y_i) - \bar{\rho}_i(t_0, y_0)}{y_i - y_0} + \bar{w}_i \frac{\bar{\rho}_i(t_i, z_i) - \bar{\rho}_i(t_0, z_0)}{z_i - z_0} \right) \frac{\Delta h_i}{h_m} + \overline{\rho w} (h_m)$$


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Gu et al 模型
Ag For Meteorol (2012)

净生态系统CO₂交换 (NEE_{CO2})

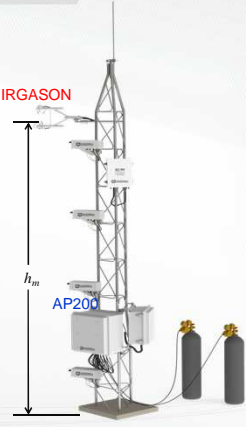
$$NEE_{CO_2} = \int_0^{h_m} \frac{\partial \bar{p}}{\partial t} dz - \frac{\bar{p}}{\rho_d} \int_0^{h_m} \frac{\partial \bar{\rho}_d}{\partial t} dz$$


$$\overline{\rho w} (h_m) + \frac{\bar{p}}{\rho_d} \overline{\rho_{H_2O} w} + \bar{\rho}_a \frac{\bar{T} w}{T}$$

净生态系统H₂O交换 (NEE_{H2O})

$$NEE_{H_2O} = \int_0^{h_m} \frac{\partial \bar{\rho}_{H_2O}}{\partial t} dz - \frac{\bar{\rho}_{H_2O}}{\rho_d} \int_0^{h_m} \frac{\partial \bar{\rho}_d}{\partial t} dz$$

$$\overline{\rho_{H_2O} w} (h_m) + \frac{\bar{\rho}_{H_2O}}{\rho_d} \overline{\rho_{H_2O} w} + \bar{\rho}_a \frac{\bar{T} w}{T}$$




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谢谢!



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